

Propositions

Definition. A *proposition* is a sentence that is either true (T) or false (F), but not both.

Examples: Which of the following are propositions? ✓• The Alamo is located in San Antonio.+ $\sqrt{-4+2} = 42$ false -• UTSA is the best school in the world. $\checkmark 2*3 = 6$ +re $- \cdot 2 * x = 6$ -• It is warm in San Antonio 8/26/09 CS 2233 Discrete Mathematical Structures -- Carola Wenk 2

Negation

Definition. Let *p* be a proposition. The *negation* ("not") of p, denoted by $\neg p$, has the opposite truth value than the truth value of p. Read $\neg p$ as: "not p" or "It is not the case that p".

Truth Table:

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Examples: Negate the following:

- ۰، The Alamo is located in San Antonio."
 - »-"The Alamo is not located in San Antonio"
 - or "It is not the case that the Alamo is located in San Antonio"
- · Today is Monday

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» "Today is not Monday" or "It is not the case that today is Monday"









Biconditional Statement \leftrightarrow

Definition. Let <i>p</i> and <i>q</i> be propositions. The		Truth Table:		
biconditional statement ("iff") $n \leftrightarrow a$ is true	p	<i>q</i>	$p \leftrightarrow q$	
when p and q have the same truth value, and	Т	Т	Т	
false otherwise.	Т	F	F	
Read $p \leftrightarrow q$ as: " <i>p</i> if and only if <i>q</i> "	F	Т	F	
"p iff q"	F	F	Т	
Example: • "You can take the flight if and only if you buy a ticket."				

 $p \oplus q$

Τ

6



