9/13/16

# 2. Homework

Due 9/22/16 at the beginning of class

## 1. BST Generator (6 points)

Describe an efficient algorithm that generates a perfectly balanced binary search tree of height h with keys 0 through  $2^{h+1} - 2$ . Your can describe the algorithm in words only. Analyze the running time.

#### 2. Heaps (6 points)

Let H be a max-heap storing n keys. Give an efficient algorithm for printing all keys in H that are greater than or equal to a given query key q. Your algorithm should run in O(k) time, where k is the number of keys printed. Justify that your algorithm has this runtime.

# 3. Bitonic (6 points)

Let A[0..n-1] be an array containing a *bitonic* sequence of n distinct numbers. A sequence is called *bitonic* if it consists of a decreasing sequence followed by an increasing sequence. For example 8, 5, 3, -1, -4, 2, 6 is bitonic, while 8, 5, 3, 2, 1, 7, 6 is not.

Describe a divide-and-conquer algorithm that finds the minimum element in a bitonic array in  $O(\log n)$  time.

## 4. Guessing and Induction (5 points)

For the recurrence below, use the recursion tree method to find a good guess of what they could solve to asymptotically (make your guess as tight as possible). Then prove that T(n) is in big-Oh of your guess by big-Oh induction; you do not have to prove the base case.

$$T(n) = 4T(n/2) + 3n$$
 for  $n \ge 1$ , and  $T(1) = 1$ .