

Answer the questions in the space provided below. You may use the back of the page if you need more space. Time: 15 minutes.

Name and section: \_\_\_\_\_

1. Let  $m, n \in \mathbb{N}_+$  be positive natural numbers. Answer the following questions (you do not have to provide proofs):
  - (a) How many edges does  $K_n$  (the complete graph on  $n$  vertices) have? (20)
  - (b) How many edges does  $K_{m,n}$  (the complete bipartite graph on  $n$  and  $m$  vertices) have? (20)
2. Let  $G$  be a non-empty graph, such that every vertex in  $G$  has degree two. Let  $e$  be an arbitrary edge of  $G$ . Prove or disprove the following statement:  $G - e$  is a connected graph. (60)