

# 4. Homework (undergrad)

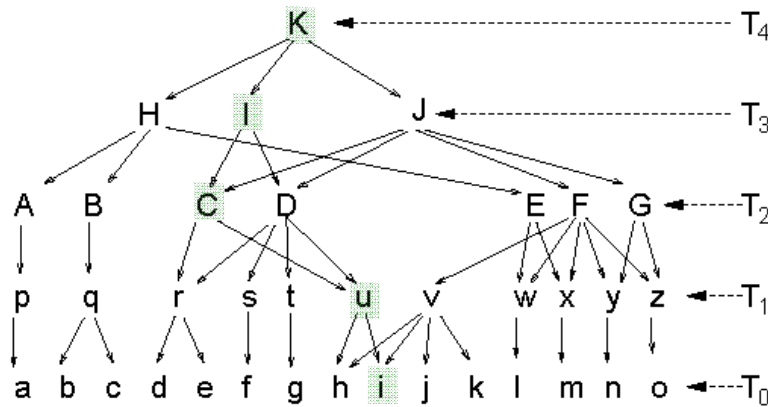
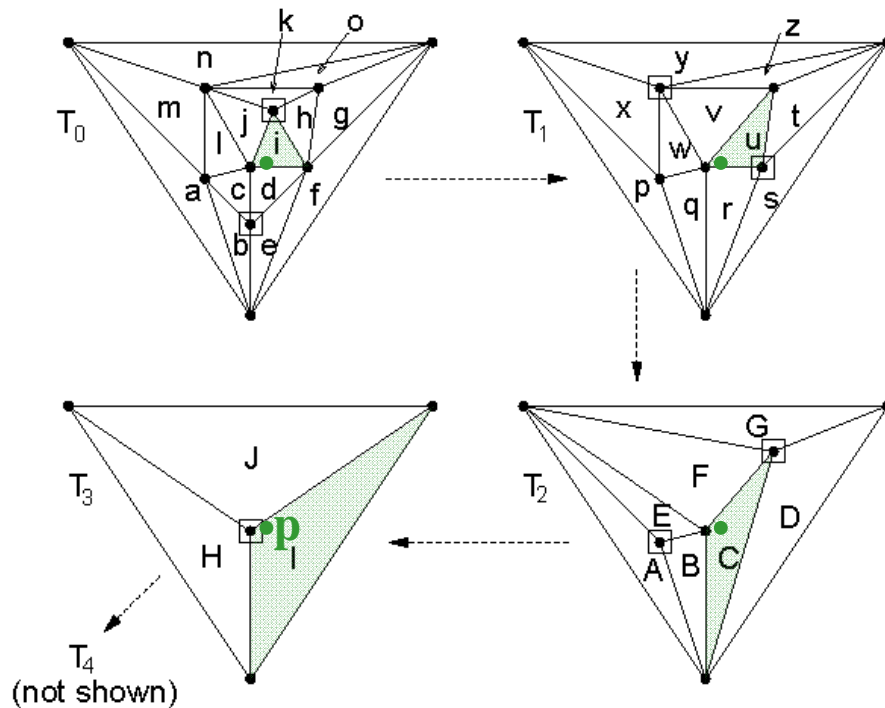
Due 2/13/20 before class

Please justify all your answers. Often it helps to draw pictures.

## 1. Kirkpatrick's Hierarchy (5 points)

Consider slide 7 of the point location II slides as well as the figure below. The path in the DAG for locating point  $p$  is  $K - I - C - u - i$ . But there are other paths in the hierarchy that also end in triangle  $i$ .

Now consider the path  $K - J - F - v - i$ . Describe where in the original triangulation a point  $p'$  has to lie such that the point location for it would follow this path.



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**2. DCEL (6 points)**

Which of the following equalities are always true? Justify your answers.

(a)  $Tw\!in(Tw\!in(\vec{e})) = \vec{e}$

(b)  $Next(Prev(\vec{e})) = \vec{e}$

(c)  $Tw\!in(Prev(Tw\!in(\vec{e}))) = Next(\vec{e})$

**3. Adjacent Vertices (10 points)**

You are given a planar subdivision in a doubly-connected edge list, and a vertex  $v$  in this DCEL. Give pseudocode to output all vertices adjacent to  $v$  in *clockwise* order. Your algorithm should run in  $O(deg(v))$  time, where  $deg(v)$  is the degree of  $v$ . (*Hint: Draw an example picture and run your algorithm on this example to make sure it works.*)